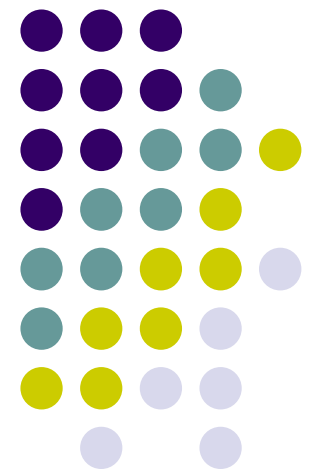
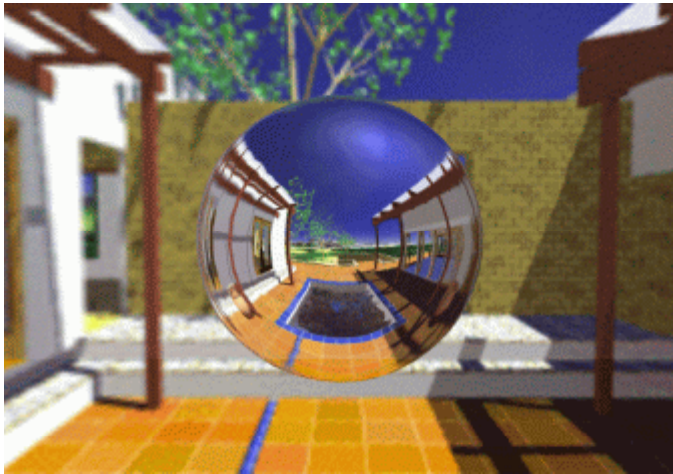
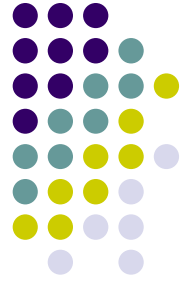


Environment Mapping

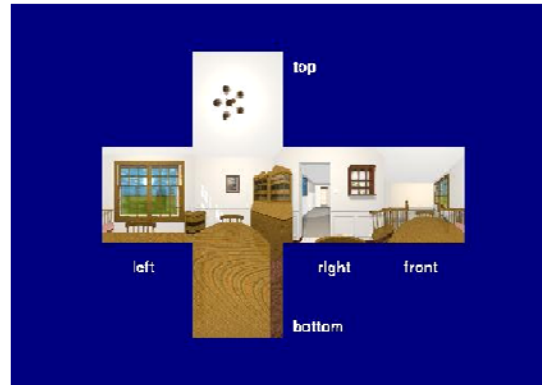
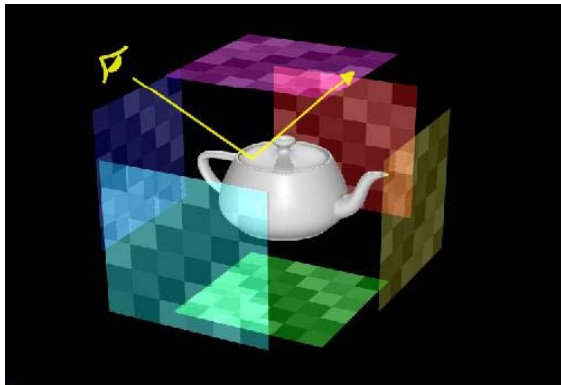


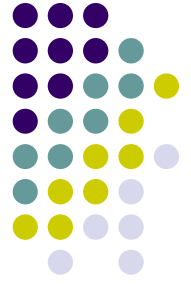
Han-Wei Shen



Environment Mapping

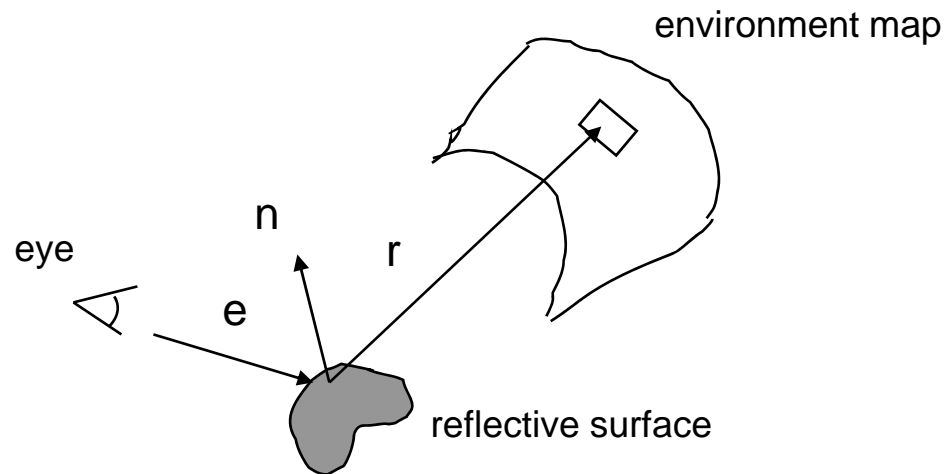
- Also called reflection mapping
- First proposed by Blinn and Newell 1976
- A cheap way to create reflections on curved surfaces – can be implemented using texture mapping supported by graphics hardware

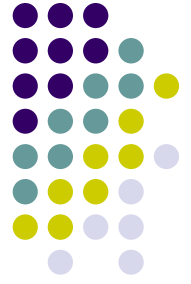




Basic Idea

- Assuming the environment is far away and the object does not reflect itself – the reflection at a point can be solely decided by the reflection vector

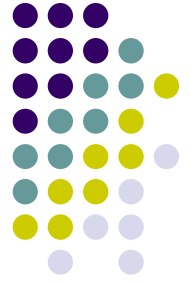




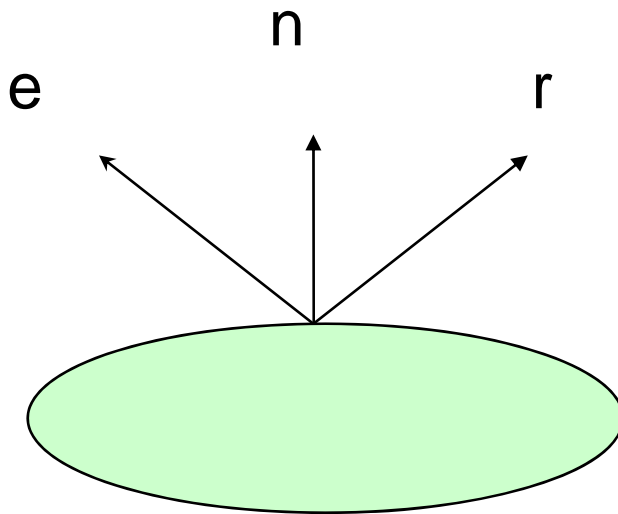
Basic Steps

- Create a 2D environment map
- For each pixel on a reflective object, compute the normal
- Compute the reflection vector based on the eye position and surface normal
- Use the reflection vector to compute an index into the environment texture
- Use the corresponding texel to color the pixel

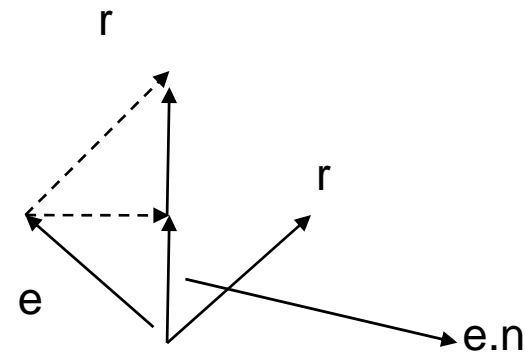
Finding the reflection vector



- $r = 2 (n \cdot e) n - e$



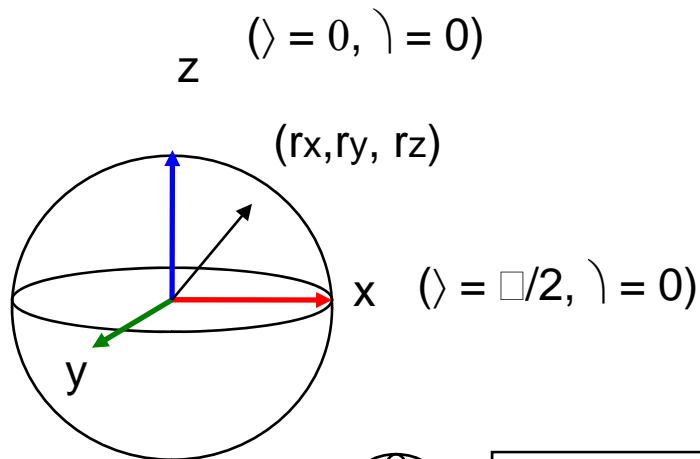
Assuming e and n are all normalized



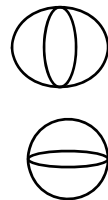


Blinn and Newell's

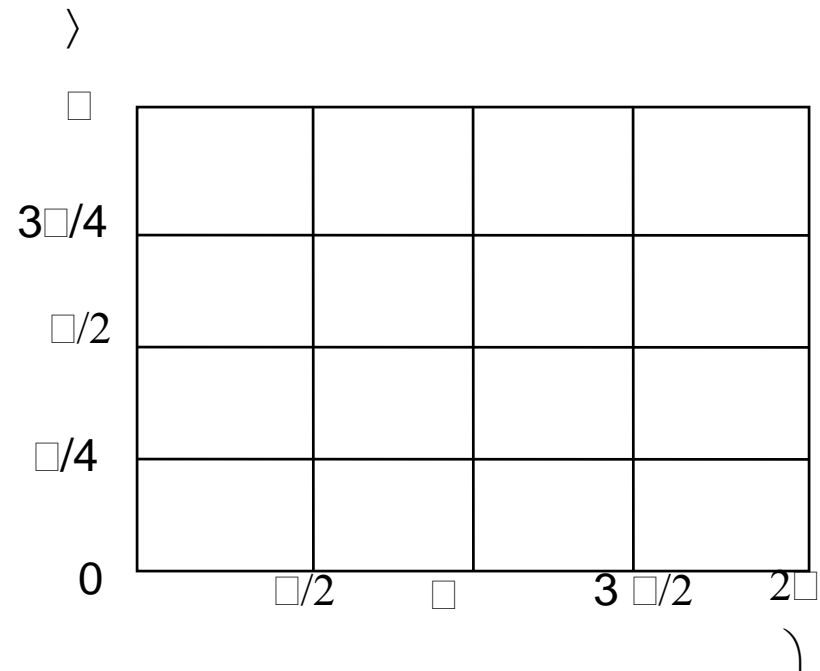
- Blinn and Newell's Method (the first EM algorithm)
- Convert the reflection vector into spherical coordinates (θ, ϕ) , which in turn will be normalized to $[0, 1]$ and used as (u, v) texture coordinates

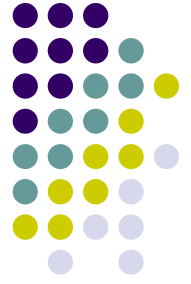


θ : latitude $[0, \pi]$
 ϕ : longitude $[0, 2\pi]$



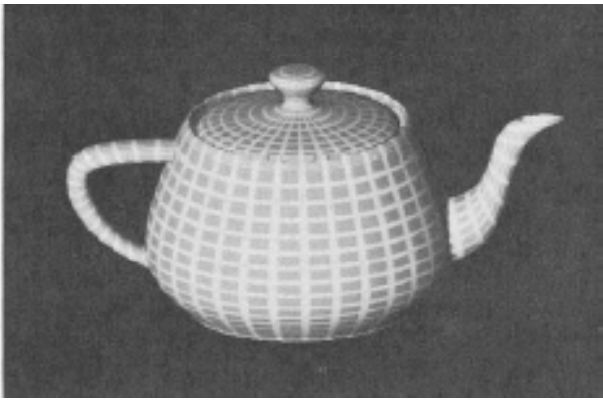
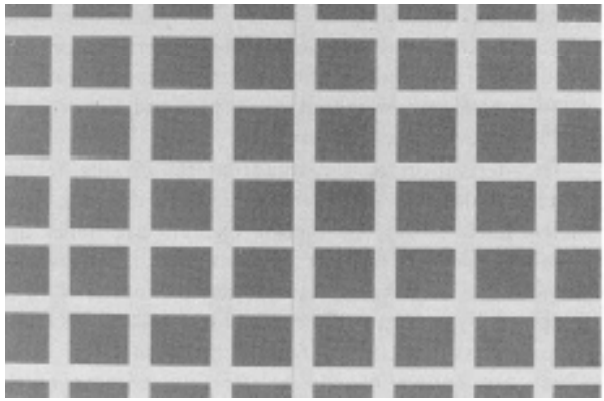
$\theta = \arccos(r_z)$
 $\phi = \text{atan2}(r_y, r_x)$





Issues

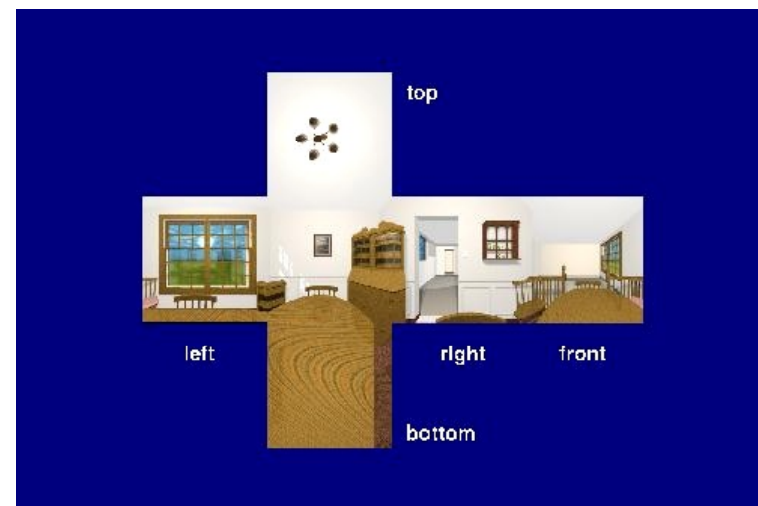
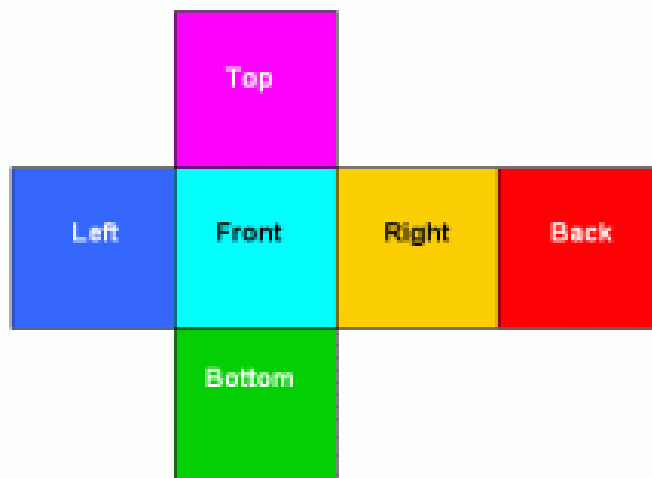
- Seams at $\lambda = 0$ when the triangle vertices span over
- Distortion at the poles, and when the triangle vertices span over
- Not really been used much in practice





Cubic Environment Mapping

- Introduced by Nate Green 1986 (also known as environment cube map)
- Place the camera in the center of the environment and project it to 6 sides of a cube

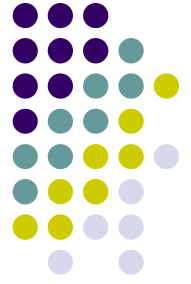


Cubic Environment Mapping (2)

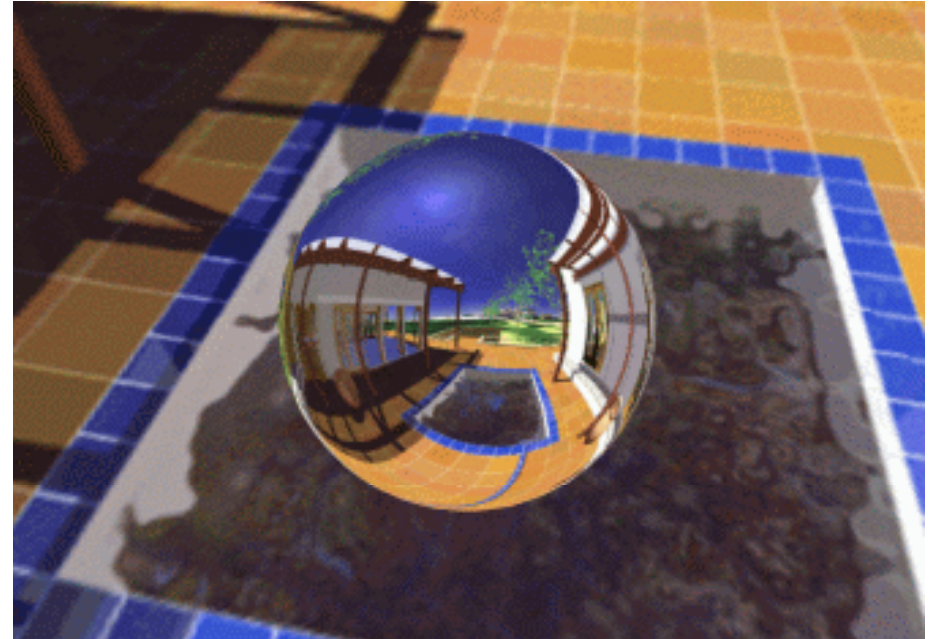
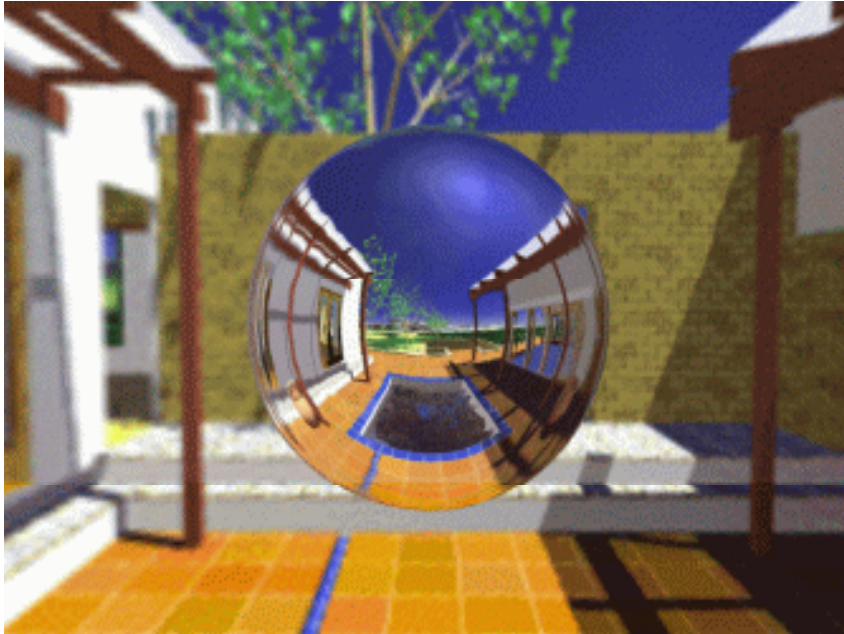


- Texture mapping process
 - Given the reflection vector (x,y,z) , first find the major component and get the corresponding plane. $(-3.2, 5.1, -8.4) \rightarrow -z$ plane
 - Then use the remaining two components to access the texture from that plane.
 - Normalize them to $(0,1)$
 - $(-3.2, 5.1) \rightarrow ((-3.2/8.4)/2+0.5, (5.1/8.4)/2+0.5)$
 - Then perform the texture lookup
- No distortion or seam problems, although when two vertices of the same polygon pointing to different planes need to be taken care of.

Environment Cube Map



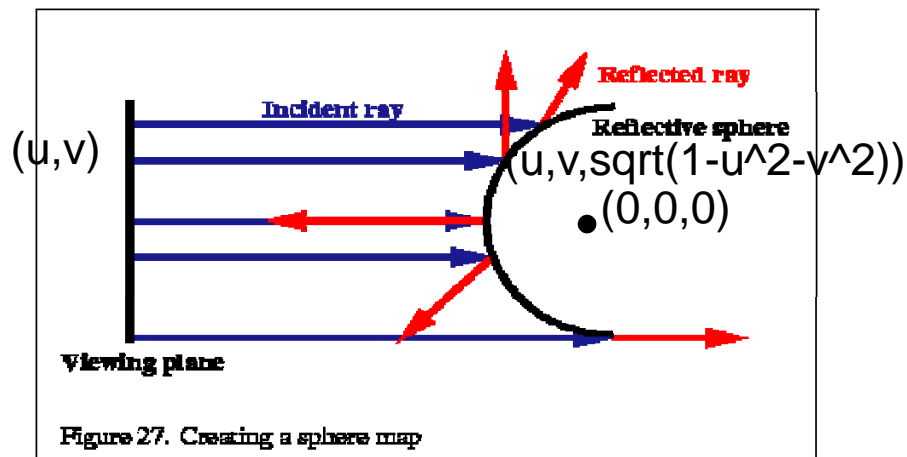
- Rendering Examples

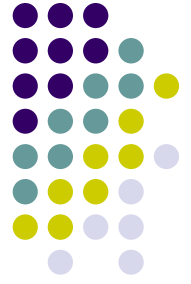


Sphere Mapping



- The image texture is taken from a perfectly reflective sphere, which is viewed from the eye orthographically.
- Synthetic scene can be
- generated using ray tracing





Sphere Mapping (2)

- To access the sphere map texture
 - The surface normal (n) and eye (e) vectors need to be first transformed to the eye space
 - Then compute the reflection vector as usual
 - $(r = (r_x, r_y, r_z) = e' - 2(n' \cdot e')n')$
 - Now, compute the sphere normal in the local space $n = (r_x, r_y, r_z) + (0, 0, 1)$
 - reflection vector
 - Directoin to the eye in local space
 - Normalize it and use x and y to access the sphere texture map: $u = r_x / M + \frac{1}{2}$; $v = r_y / M + \frac{1}{2}$;
 - where $M = 2 \sqrt{r_x^2 + r_y^2 + (r_z + 1)^2}$