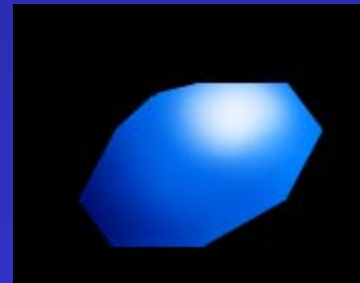
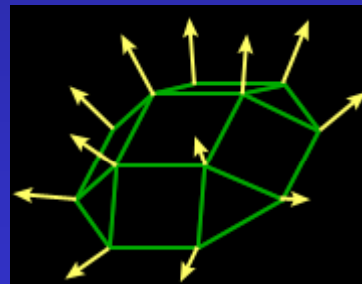
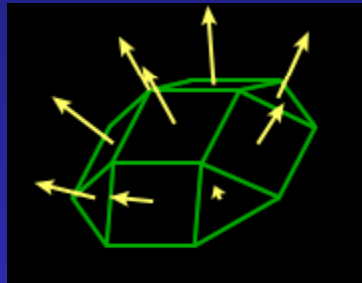


Smooth Shading

Gouraud

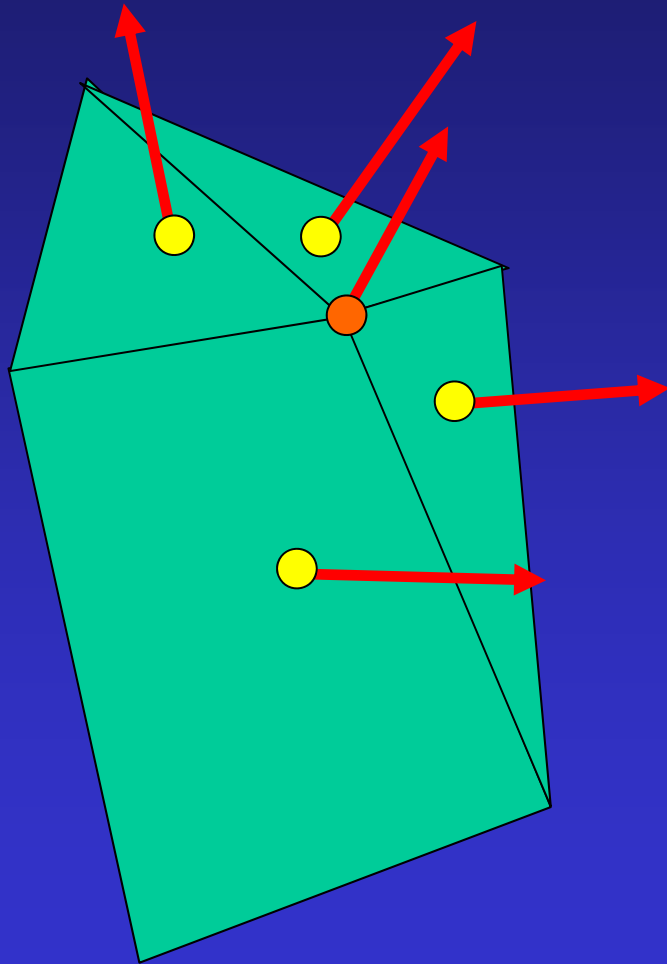
Phong

Interpolate value(s) for point in face from values at vertices



<http://www.blancmange.info/notes/maths/vectors/primitives/>

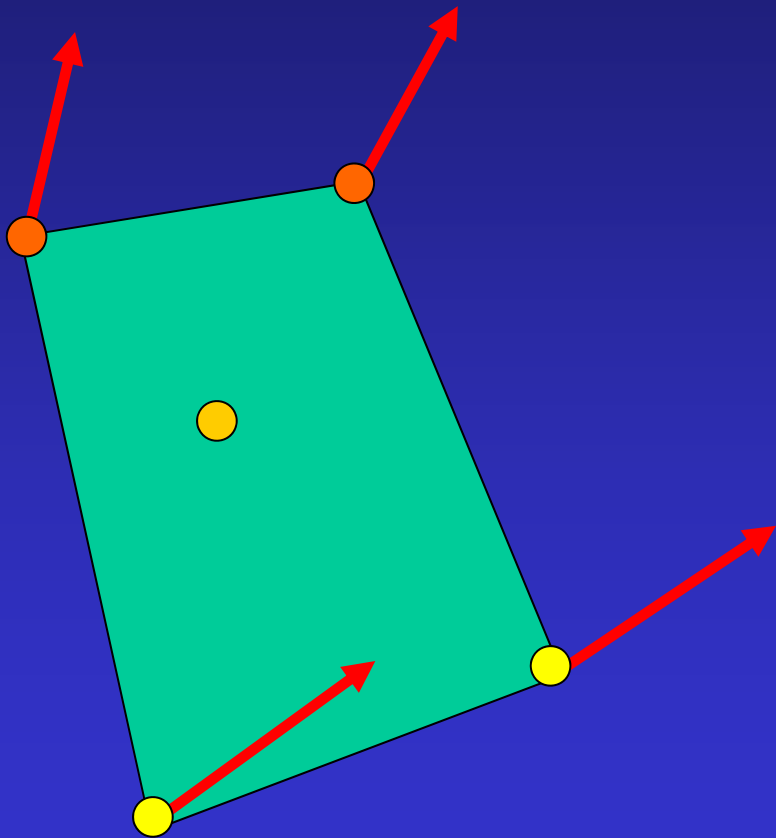
Compute normals at vertices



For each vertex, v
 $N_v = \langle 0, 0, 0 \rangle$
For each face of vertex
 Compute face normal
 $N_v += \text{face normal}$
Normalize N_v

For each vertex, v
 $N_v = \langle 0, 0, 0 \rangle$
For each face
 Compute face normal
 For each vertex of face
 $N_v += \text{face normal}$
For each vertex, v
Normalize N_v

Interpolate value(s) for point in face from values at vertices



Gouraud smooth shading:

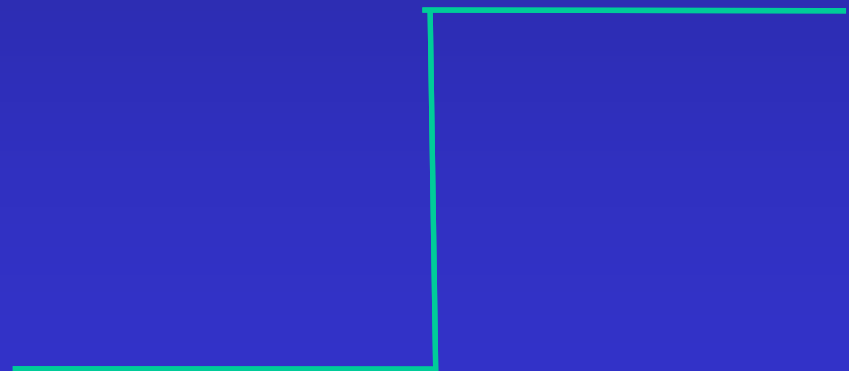
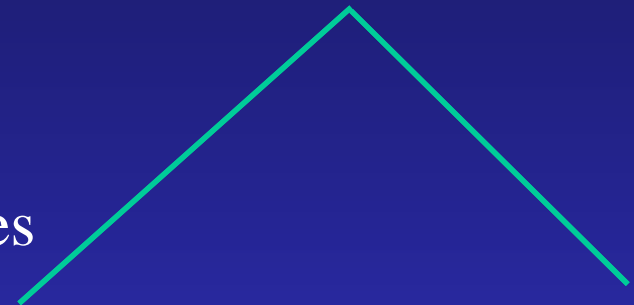
1. Compute normals at vertices
2. Compute color at vertices
3. Interpolate interior color

Mach Band Effect

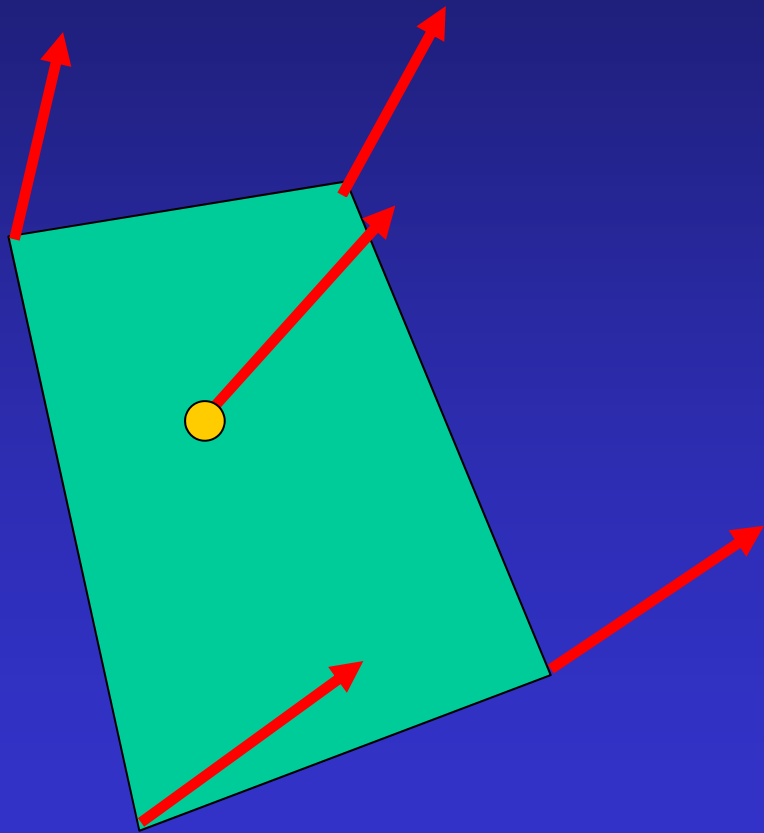
Smoothly shaded objects

Colors are continuous, but not derivatives

Eye picks up on this and accentuates discontinuity



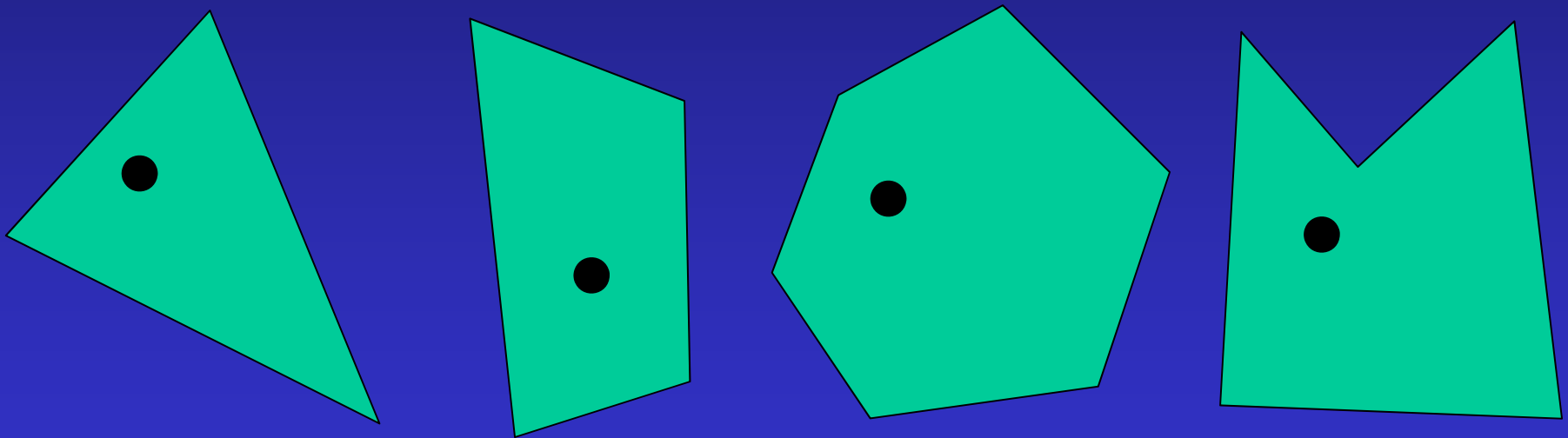
Interpolate value(s) for point in face from values at vertices



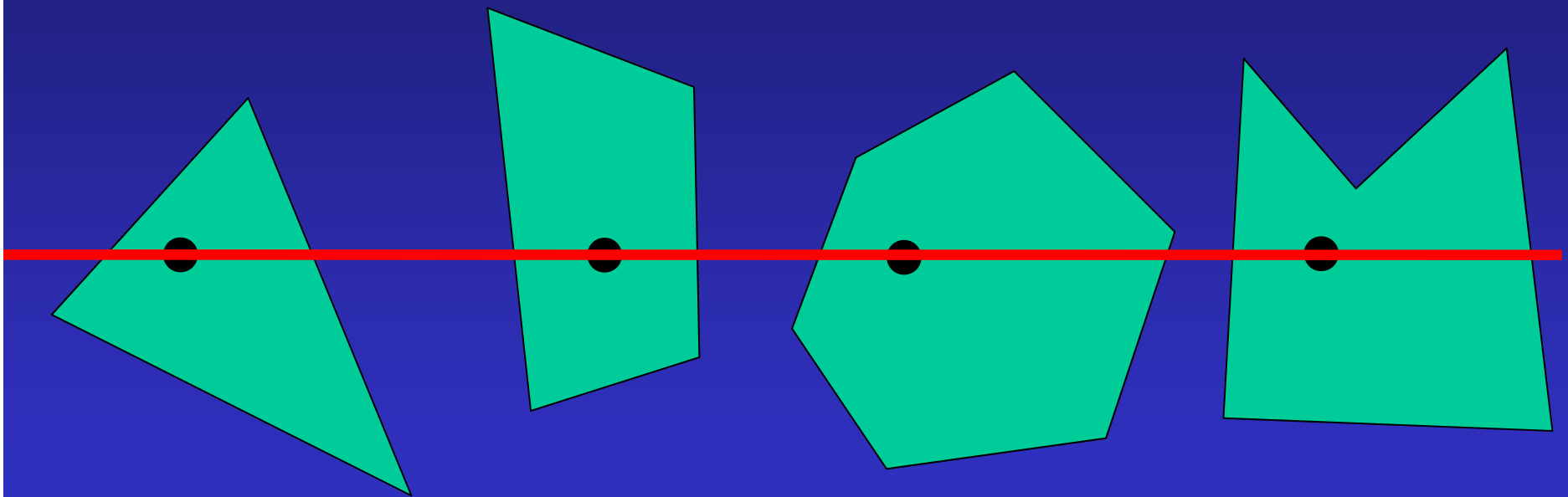
Phong smooth shading:

1. Compute normals at vertices
2. Interpolate interior normal
3. Compute color at point

Interpolate value(s) for point in face from values at vertices

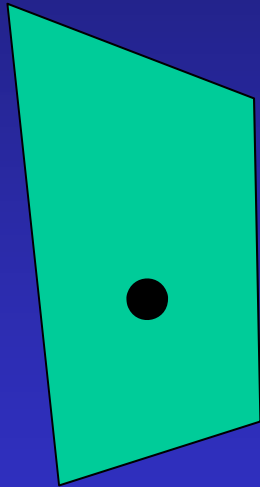


Interpolate value(s) scanline algorithms



Interpolate down edges, across scanline

Point sample Quadrilateral inverse bilinear map then use u, v values to interpolate



$$P_{u0} = (1-u)P_{00} + uP_{10}$$

$$P_{u1} = (1-u)P_{01} + uP_{11}$$

$$P_{uv} = (1-v)P_{u0} + vP_{u1}$$

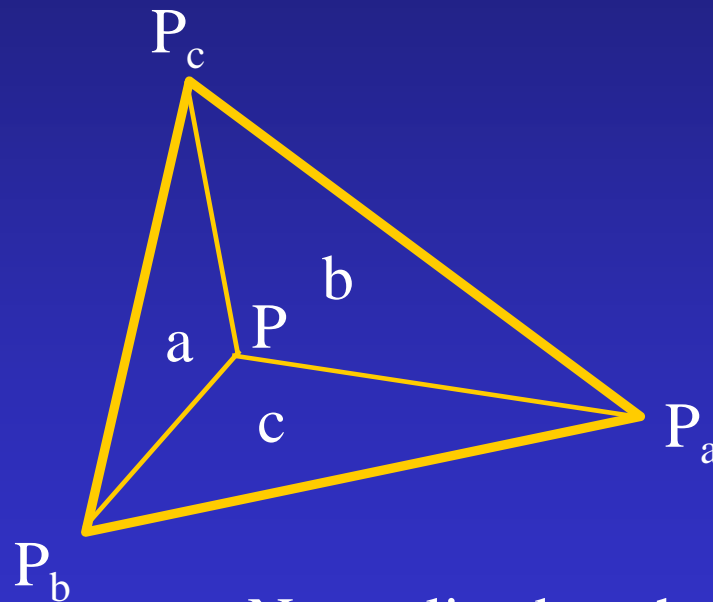
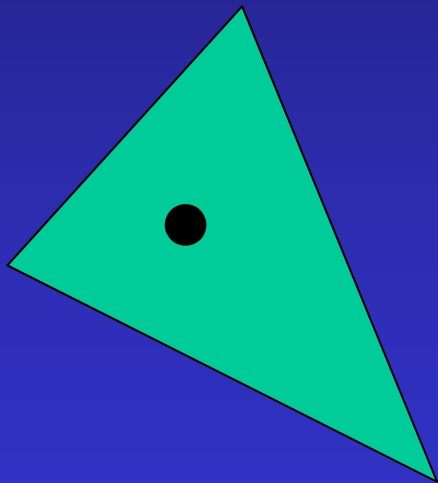
$$P_{uv} = (1-v)((1-u)P_{00} + uP_{10}) + v((1-u)P_{01} + uP_{11})$$

$$P_{uv} = vu(P_{11} - P_{01} - P_{10} + P_{00}) + v(P_{01} - P_{00}) + u(P_{10} - P_{00}) + P_{00}$$

$$u = \frac{P_{uv} - P_{00} - v(P_{01} - P_{00}) - P_{00}}{v(P_{11} - P_{01} - P_{10} + P_{00}) + (P_{10} - P_{00})}$$

Point sample Triangle

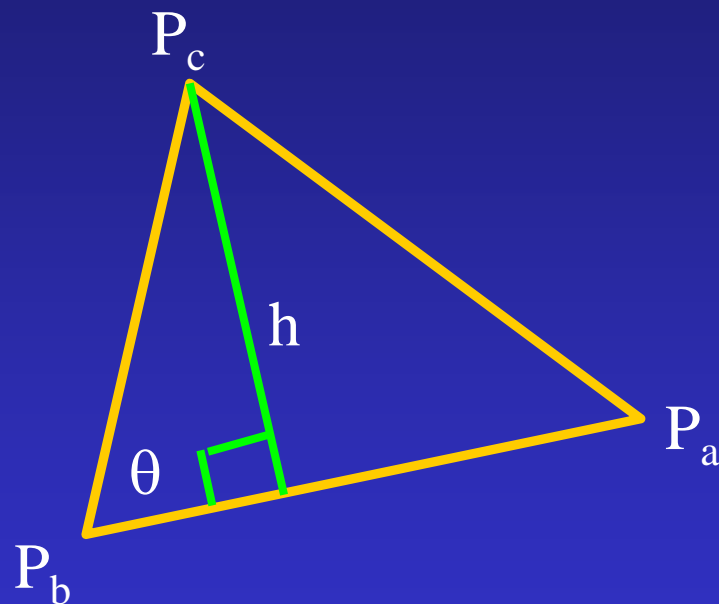
compute barycentric coordinates
then use to interpolate



Normalized so that $a+b+c=1$

$$P = aP_a + bP_b + cP_c$$

Area of a triangle - using vector algebra



$$\text{Area} = (1/2)h|\mathbf{V}_{ab}|$$

$$h = |\mathbf{V}_{bc}| \sin(\theta)$$

$$\text{Area} = (1/2) |\mathbf{V}_{ab}| |\mathbf{V}_{bc}| \sin(\theta)$$

$$|\mathbf{V}_{ab} \times \mathbf{V}_{bc}| = |\mathbf{V}_{ab}| |\mathbf{V}_{bc}| \sin(\theta)$$

$$\text{Area} = (1/2) |\mathbf{V}_{ab} \times \mathbf{V}_{bc}|$$

Examples of smooth shading

See links off of course web site