

# Deformable Models

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# Deformation

- Definition from engineering mechanics - change in shape or volume due to an applied force
- Can be a result of tensile (pulling) forces, compressive (pushing) forces, shear, bending or torsion (twisting)
- Real objects are flexible, not rigid
- Deformable objects exhibit complex motion that is tedious to animate by hand
- Animating humans and animals
- The challenge - create efficient and user-friendly methods of simulating deformable characters

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# Gradient Domain Editing of Deforming Mesh Sequences (SIGGRAPH 2007)

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- Generalizes gradient domain static mesh editing to deforming mesh sequences
- Keyframe based
- Goal
  - Adapt existing deforming mesh sequences to conveniently produce desired ones that satisfy both user and environment requirements
  - Minimize user intervention
  - System should permit flexible and precise user control
  - Given very sparse constraints, results should preserve both temporal coherence and important characteristics of deformations in original mesh sequences

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# Gradient Domain Editing of Deforming Mesh Sequences

Related work

- Previous work on surface and meshless deformations [Alexa 2003, Sheffer and Kraevoy 2004, Huang et al. 2006 ...]
- Multiresolution mesh editing [Zorin et al. 1997, Kobbelt et al. 1998 ...]
- Mesh inverse kinematics [Sumner et al. 2005 ...]



# Gradient Domain Editing of Deforming Mesh Sequences

Editing deforming mesh sequences

- User chooses to edit an arbitrary subset of frames. Each edited frame becomes a keyframe
- At each keyframe, user can also edit an arbitrary subset of handles
- Handle - subset of nearby vertices within the same frame
- For manipulating a handle, user only needs to drag one vertex in the handle to provide a positional constraint

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## Advanced editing

- E.g. porting a walking sequence from a plane to an uneven terrain would require a lot of user interaction
- Hence advanced editing modes are built on top of the editing framework
  - Footprint editing
  - Path editing
  - Handle-based deformation mixing - Duplicating handle movements from a source sequence to a target sequence
  - Spacetime morphing

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# Gradient Domain Editing of Deforming Mesh Sequences

## Footprint editing

- During walking or running, at least one support leg in contact with ground - footprint
- Interval of frames where a handle remains fixed on the ground
- User defines handle that represents the foot.
- Detected by checking in what interval the position of the handle is unchanged or changes are less than a threshold
- Frames with footprints are set as keyframes
- Time saved by editing one handle at several frames simultaneously
- Footprints correctly capture constraints that should be satisfied in walking motion

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# Gradient Domain Editing of Deforming Mesh Sequences

## Path editing

- User only needs to sketch a curve on the ground as a new motion path
- Projects centroids of meshes in original sequence onto ground
- Fits a B-spline curve through these projected points
- Builds correspondence between original path and new one using arc length

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# Gradient Domain Editing of Deforming Mesh Sequences

## Handle-based deformation mixing

- Start with two deforming meshes and generate a new sequence that mixes the large-scale deformations of the first with the small-scale deformations of the second
- Uses motion trajectories of a sparse set of handles on the first mesh to define its large-scale deformations
- Forces the corresponding handles on the second mesh to follow these trajectories
- Align two corresponding trajectories using a global transformation
- Set transformed handle positions and rotations from first trajectory as constraints for corresponding handle on the second mesh

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## Spacetime morphing

- Morphs a source deforming mesh  $A^s$  to a target deforming mesh  $A^t$  in terms of both shape and deformation
- E.g. A walking dinosaur morphs into a walking lion
- Preprocessing step - Both sequences are remeshed so that every pair of corresponding frames have same topology
- Uses cross-parametrization from [Kraevoy and Sheffer 2004]
- Constraints such as footprints should be handled in spacetime morphing as well

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# Gradient Domain Editing of Deforming Mesh Sequences

## Results

- Editing session has both online and offline stages
- Online keyframe editing - interactive frame rates using approximate initial solutions
- Followed by offline computation to obtain entire edited sequence
- Horse sequence - 29k triangles, 420 frames, 50 minutes of precomputation time, 30 minutes for solution, 1 hr session time (on a 3.2 GHz Intel Xeon with 4 GB memory). Includes virtual memory paging time

# Gradient Domain Editing of Deforming Mesh Sequences

## Summary

- Novel editing scenarios
- Intuitive editing
- Multithreading and novel acceleration techniques to improve performance



# Embedded Deformation for Shape Manipulation (SIGGRAPH 2007)

Robert W. Sumner, Johannes Schmid, Mark Pauly  
Applied Geometry Group, ETH Zurich

# Embedded Deformation for Shape Manipulation

## Introduction

- Embedded deformation - Deform space through direct manipulation of objects embedded within it, while preserving objects' features
- Motivation
  - Generality - Wide range of shape representations. Defined by affine transformations
  - Efficiency - Simple, general and independent of any particular geometry representation
  - Detail preservation - Small scale details should be preserved when a broad change in shape is made
  - Direct manipulation - Optimization problem where positional constraints are specified

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## Background

- Related work
  - Singh and Fiume, 1998 - 'Wires' concept motivated by armatures used in traditional sculpting
  - Huang et al., 2006 - Subspace method for increased efficiency and stability
  - Sheffer and Kraevoy, 2004 - Nonlinear methods - highest quality at higher computational costs
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# Embedded Deformation for Shape Manipulation

## Deformation graph

- Space deformation represented by a collection of affine transformations organized in a graph structure.
- Each transformation induces a deformation on the nearby space
- Nodes ( $g_j$ ) are connected by undirected edges
- Graph edges connect nodes of overlapping influence to indicate local dependencies
- Affine transformation for node  $j$  is specified by a 3x3 matrix  $R_j$  and a 3x1 translation vector  $t_j$
- $\tilde{p} = R_j(p-g_j) + g_j + t_j$

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## Results

- Detail preservation - Comparable or better results than previous work
- Intuitive editing - High quality edits by using a handful of single-vertex handle constraints
- Mesh animation - Online and offline mode. Preserves geometric details.
- Efficiency - Interactive performance

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# Embedded Deformation for Shape Manipulation

## Summary

- Comparable or better than existing methods
- Applies to variety of shapes
- Deformation graph is easy to construct and corresponds closely to embedded shape
- Complexity of deformation algorithm is not tied to geometric complexity of the embedded object

# References

- Wikipedia - Interactive\_skeleton-driven\_simulation, Skeletal\_animation, Deformation
- <http://grail.cs.washington.edu/projects/deformation/>