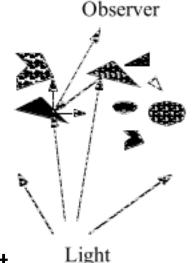
Fundametals of Rendering -Radiometry / Photometry

"Physically Based Rendering" by Pharr & Humphreys

- Chapter 5: Color and Radiometry
- Chapter 6: Camera Models we won't cover this in class

Realistic Rendering

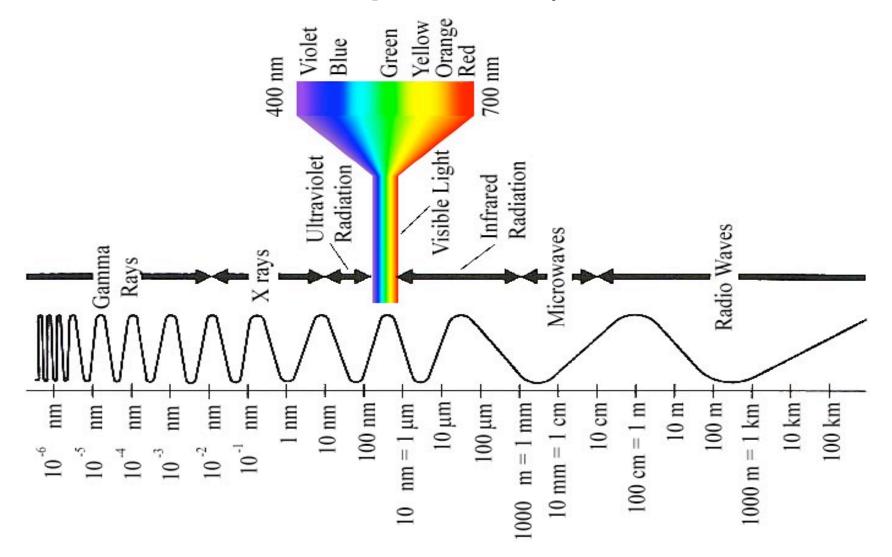
- Determination of Intensity
- Mechanisms
 - Emittance (+)
 - Absorption (-)
 - Scattering (+) (single vs. multiple)
- Cameras or retinas record quantity of light



Pertinent Questions

- Nature of light and how it is:
 - Measured
 - Characterized / recorded
- (local) reflection of light
- (global) spatial distribution of light

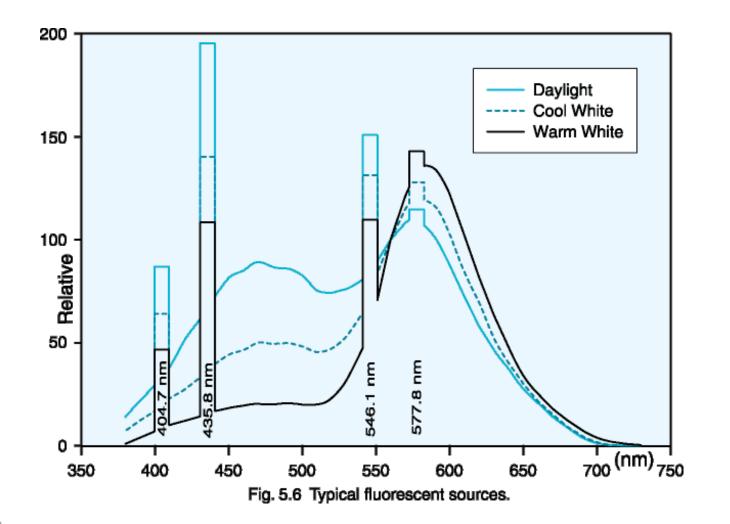
Electromagnetic spectrum



782

Spectral Power Distributions

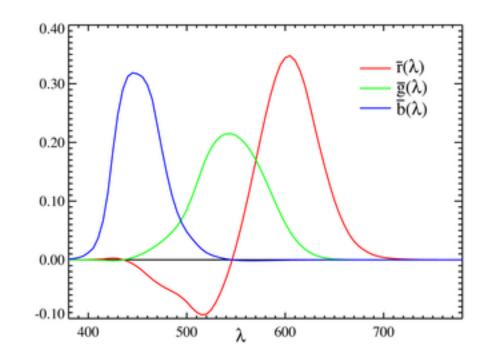
e.g., Fluorescent Lamps



782

Tristimulus Theory of Color

Metamers: SPDs that appear the same visually



Color matching functions of standard human observer International Commision on Illumination, or CIE, of 1931

"These color matching functions are the amounts of three standard monochromatic primaries needed to match the monochromatic test primary at the wavelength shown on the horizontal scale." from Wikipedia "CIE 1931 Color Space"

Optics

Three views

Geometrical or ray

- Traditional graphics
- Reflection, refraction
- Optical system design

• Physical or wave

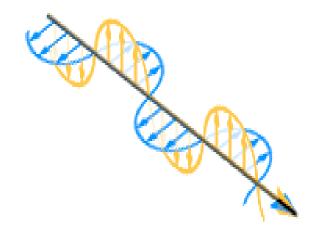
- Dispersion, interference
- Interaction of objects of size comparable to wavelength

Quantum or photon optics

- Interaction of light with atoms and molecules

What Is Light ?

- Light particle model (Newton)
 - Light travels in straight lines
 - Light can travel through a vacuum (waves need a medium to travel in)
 - Quantum amount of energy
- Light wave model (Huygens): electromagnetic radiation: sinusiodal wave formed coupled electric (E) and magnetic (H) fields



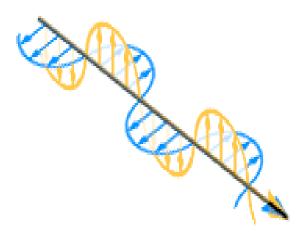
Nature of Light

• Wave-particle duality

- Light has some wave properties: frequency, phase, orientation
- Light has some quantum particle properties: quantum packets (photons).

Dimensions of light

- Amplitude or Intensity
- Frequency
- Phase
- Polarization



Nature of Light

- **Coherence** Refers to frequencies of waves
- Laser light waves have uniform frequency
- Natural light is incoherent- waves are multiple frequencies, and random in phase.
- **Polarization** Refers to orientation of waves.
- Polarized light waves have uniform orientation
- Natural light is unpolarized it has many waves summed all with random orientation
- Focused feflected light tends to be parallel to surface of reflection

Radiometry

- Science of measuring energy (light in our case)
- Analogous science called **photometry** is based on human perception.

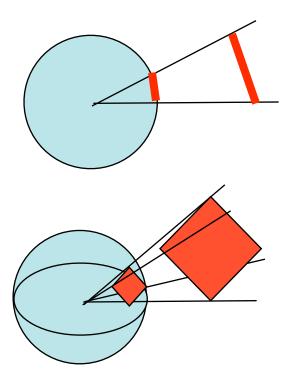
Radiometry Questions

- Measure energy leaving a light source, as a function of direction
- Measure energy hitting a surface, in a particular direction
- Measure energy leaving a surface, in a particular direction

The energy is light, photons in this case

Solid Angle

First, need to define 3D angular units



2D full circle - 4π radians

3D full sphere - 4π steradians

Terminology

Energy

Radiant energy

Power Energy per unit of time

Power on a surface

Flux Radiant power passing through a surface

Flux density Radiant power per unit area on a surface

Incident flux density

Exitant flux density (aka Radiosity)

Flux density arriving at a surface in all directions

Flux density leaving from a surface in all directions

Power in a direction

Radiant intensity

Power per unit solid angle

Radiance

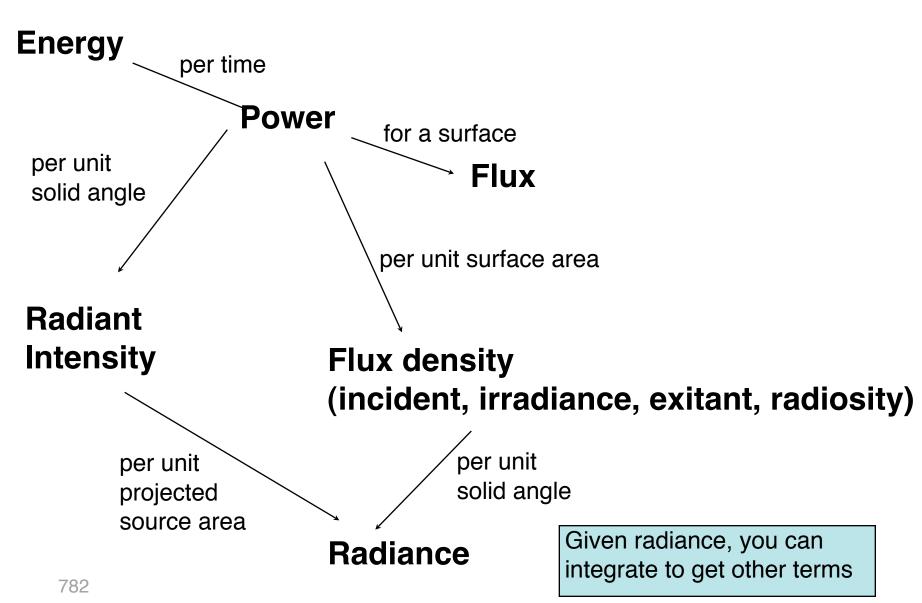
Power radiated per unit solid angle per unit projected source area

for rendering: important when considering the direction toward the camera

Radiometry - Quantities

- Energy Q
- Power Φ
 - Energy per time
- Irradiance E and Radiosity B
 - Power per area
- Intensity |
 - Power per solid angle
- Radiance L
 - Power per projected area and solid angle

Terms & Units

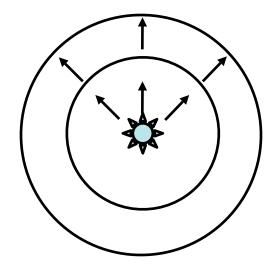


Radiant Energy - Q

- Think of photon as carrying quantum of energy
- Wave packets
- Total energy, Q, is then energy of the total number of photons
- Units joules or eV

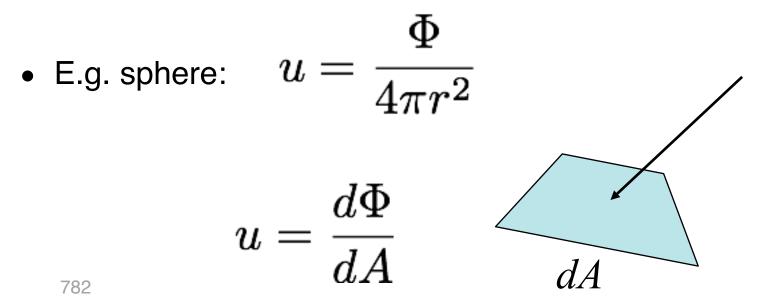
Power - Ф

- Flow of energy (important for transport)
- Also radiant power or flux.
- Energy per unit time (joules/s = eV/s)
- Unit: W watts
- $\Phi = dQ/dt$
- Falls off with square of distance



Radiant Flux Area Density or simply flux density

- Area density of flux (W/m²)
- u = Energy arriving/leaving a surface per unit time interval
- dA can be any 2D surface in space



Irradiance E

• Power per unit area incident on a surface

$E = \frac{d\Phi}{dA}$

Radiosity or Radiant Exitance B

- Power per unit area leaving surface
- Also known as Radiosity
- Same unit as irradiance, just direction changes

$$B = \frac{d\Phi}{dA}$$

Intensity I

• Flux density per unit solid angle

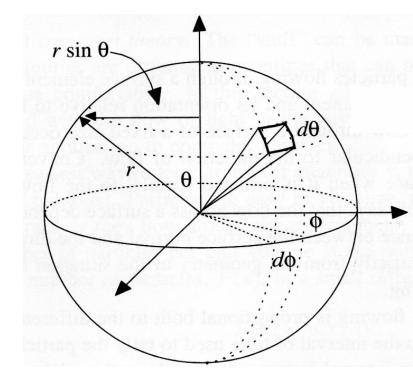
$$I = \frac{d\Phi}{d\omega}$$

- Units watts per steradian
- Radiant intensity
- "intensity" is heavily overloaded. Why?
 - Power of light source
 - Perceived brightness

Solid Angle

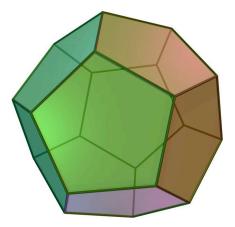
- Size of a patch, dA, in terms of its angular direction, is $dA = (r \sin \theta d\phi)(rd\theta)$
- Solid angle is

$$d\omega = \frac{dA}{r^2} = \sin\theta d\theta d\phi$$



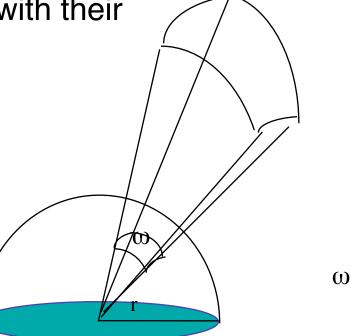
Solid Angle (contd.)

- Solid angle generalizes angle!
- Steradian
- Sphere has 4π steradians! Why?
- Dodecahedron 12 faces, each pentagon.
- One steradian approx equal to solid angle subtended by a single face of dodecahedron



Hemispherical Projection

- Use a hemisphere H over surface to measure incoming/outgoing flux
- Replace objects and points with their hemispherical projection



Isotropic Point Source

$$I = \frac{d\Phi}{d\omega} = \frac{\Phi}{4\pi}$$

• Even distribution over sphere

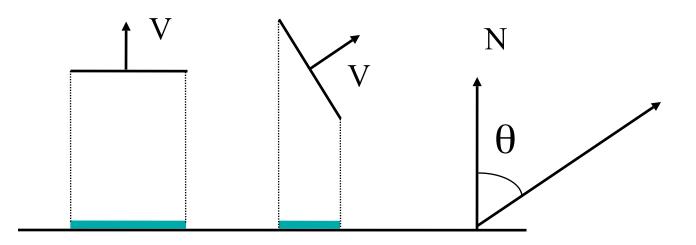
Radiance L

- Power per unit projected area per unit solid angle.
- Units watts per (steradian m²)
- We have now introduced projected area, a cosine term.

$$L = \frac{d^2 \Phi}{dA_p d\omega} \qquad \qquad L = \frac{d^2 \Phi}{dA \cos \theta d\omega}$$

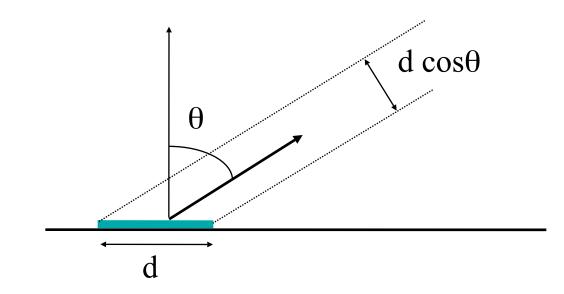
Projected Area

$A_p = A(N \cdot V) = A\cos\theta$



Why the Cosine Term?

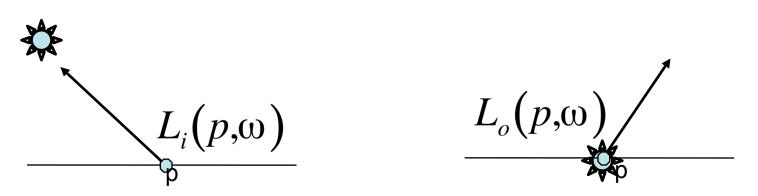
- Foreshortening is by cosine of angle.
- Radiance gives energy by effective surface area.



Incident and Exitant Radiance

- Incident Radiance: L_i(p, ω)
- Exitant Radiance: $L_{o}(p, \omega)$
- In general: $L_i(p,\omega) \neq L_o(p,\omega)$
- p no surface, no participating media

$$L_i(p,\omega) = L_o(p,-\omega)$$

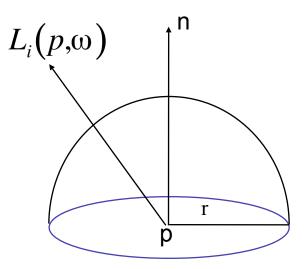


Note that direction is always **away** from point

Irradiance from Radiance

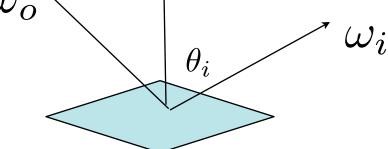
$$E(p,n) = \int_{\Omega} L_i(p,\omega) |\cos \theta| d\omega$$

- $lcos\theta ld\omega$ is projection of a differential area
- We take lcosθl in order to integrate over the whole sphere



Reflected Radiance & BRDFs

 $dL_o(p,\omega_o) \propto dE(p,\omega_i)$ Ν ω_o



$$f_r(p,\omega_o,\omega_i) = \frac{dL_o(p,\omega_o)}{dE(p,\omega_i)} = \frac{dL_o(p,\omega_o)}{L_i(p,\omega_i)\cos\theta_i d\omega_i}$$

Bidirectional Reflection Distribution Functions

Reciprocity: $f_r(p, \omega_i, \omega_o) = f_r(p, \omega_o, \omega_i)$

Energy Conservation:

$$\int_{H^2(n)} f_r(p, \omega_o, \omega') \cos \theta' d\omega' \le 1$$

Bidirectional Scattering Distribution Functions

Bidirectional Reflection Distribution Function (BRDF)

$$f_r(p, \omega_o, \omega_i)$$

Bidirectional Transmittance Distribution Function (BTDF)

$$f_t(p, \omega_o, \omega_i)$$

Bidirectional Scattering Distribution Function (BSDF)

$$f(p, \omega_o, \omega_i)$$

Bidirectional Scattering Distribution Functions

$$dL_o(p,\omega_o) = f(p,\omega_o,\omega_i)L_i(p,\omega_i)|\cos\theta_i|d\omega_i$$

$$L_o(p,\omega_o) = \int_{S^2(n)} f(p,\omega_o,\omega_i) L_i(p,\omega_i) |\cos\theta_i| d\omega_i$$