Ray Tracing Implicit Surfaces

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Overview

- Similar to CSG
 - Combine primitive objects to form complex object
- Primitives are "density fields"
- Combine by **<u>summing</u>** densities
- The surface is all points at which the density equals a user-defined <u>threshold</u>

Implicit Surface

- A surface not explicitly represented
- The surface consists of all points which satisfy a function
 - $F(\mathbf{x},\mathbf{y},\mathbf{z})=0$
- Usually, the implicit function is defined so that F(x,y,z) < 0 => inside the object F(x,y,z) > 0 => outside the surface Sometimes F(x,y,z) is based on a distance-to-a-central-element
- The surface points have to be searched for!



Multiple Implicits

- Define each primitive as positive density field
- Sum densities
- Surface is defined at threshold
- Usually have finite radius of influence



Organic shapes









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Density Functions

Define a density function that is: Easy to evaluate Blends smoothly Intuitive to use

Density functions proposed in the literature Exponential Piecewise cubic Cubic in distance squared

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Distance-based Density Functions

$d_i(p) = D(|P\text{-}C_i|/R) = D(r)$

r is normalized distance

$D_1(r) = (1-r^2)^3$		0 <= r < 1
$D_2 (r) = 1 - (4/9)r^6 + (17/9)r^4 - (22/9)r^2$		0 <= r < 1
$D_3(r) = exp(-ar^2)$		
$D_4(r) = 1-3r^2$	0 <= r < 1/3	
(3/2)(1-r) ²	1/3 <= r < 1	



















Computing the Normal

Form analytic expression of implicit function And take partial derivatives $N = (\delta F/\delta x, \, \delta F/\delta y, \, \delta F/\delta z)$

Take discrete approximation by sampling function Compute gradient N = (F(x+dx,y,z)-F(x,y,z), F(x,y+dy,z)-F(x,y,z), F(x,y,z+dz)-F(x,y,z)

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CSG-approach to control blending



Use nodes to combine primitives by either summing or taking max of functions

Complexity

•Bounding volumes

•Spatial subdivision - cellular bucket sort

•Hierarchical spatial subdivision – quadtree

•Binary spatial partitioning

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Display alternative

Marching cubes algorithm - construct surface fragments from isosurface intersections with grid cells









