## Something noteworthy

- Very very noteworthy ...
- OpenGL postmultiply each new transformation matrix $M=M \times$ Mnew
- Example: perform translation, then rotation

0) $M=I$ dentity
1) translation $T(t x, t y, 0) \quad->M=M x T(t x, t y, 0)$
2) rotation $R(\theta)->M=M \times R(\theta)$
3) Now, transform a point $P \rightarrow P^{\prime}=M \times P$ $=T(t x, t y, 0) \times R+\theta) \times P$ Wrong!!!

## Example Revisit

- We want rotation and then translation
- Generate wrong results if you do:



## How Strange ...

- OpenGL has its reason ...
- It wants you to think of transformation in a different way
- Instead of thinking of transform the object in a fixed global coordinate system, you should think of transforming an object as moving (transforming) its local coordinate system


## OpenGL Transformation

- When use OpenGL, we need to think object transformations as moving (transforming) its local coordinate frame
- All the transformations are performed relative to the current coordinate frame origin and axes





## Put it all together

When you use OpenGL ...

- Think of transformation as moving coordinate frames
- Call OpenGL transformation functions in that order
- OpenGL will actually perform the transformations in the reverse order
- Everything will be just right!!!


## Change Coordinate System (1)

- What constitutes a coordinate system?
- Origin O
- Basis vector $\vec{i}, \vec{j}$


Any point $P(x, y)$ in the coordinate system can be represented:
$P=0+x * \vec{i}+y * \vec{j}$



## Change Coordinate System (4)

- What does it have anything to do with object transformation?
- We can view transformation as moving the coordinate system (reference frame) and tie the object with that frame

$$
\left|\begin{array}{l}
a \\
b \\
1
\end{array}\right|=M \quad x\left|\begin{array}{ll}
c \\
d \\
1
\end{array}\right|
$$

What is $(a, b)$ ? The coordinates Of the point $P(c, d)$ in $C$ after the coordinate system change
i.e, the new coordinates after transforming $(c, d)$


## Look at transformation again (3)

- In other words: If you think of transformations as changing coordinate frames, the order that you specify the transformations (for the frames) will be exactly opposite to the order that the transformations are actually applied (i.e. matrix- multiplied) to the object


