## Stack



## Stack

- The Stack component family allows you to manipulate strings of entries of any (arbitrary) type in LIFO (last-in-first-out) order
- A kind of "dual" to Queue
- Remember, "first" and "last" here refer to the temporal order in which entries are put into the string and taken out of it, not about the order in the string when it is written down


## Interfaces and Classes



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## Mathematical Model

- The value of a Stack variable is modeled as a string of entries of type $T$
- Formally:
type Stack is modeled by
string of $T$


## No-argument Constructor

- Ensures:
this $=<>$


## Example

| Code | State |
| :---: | :---: |
|  |  |
| Stack<Integer> si $=$ <br> new Stack1L<>(); |  |
|  |  |

## Example

| Code | State |
| :---: | :---: |
|  |  |
| Stack<Integer <br> new si stack1L<>(); | si $=<>$ |
|  |  |

## push

void push (T x)

- Adds x at the top (left end) of this.
- Aliases: reference x
- Updates: this
- Ensures:

$$
\text { this }=<x>\text { * \#this }
$$

## Example

| Code | State |
| :---: | :---: |
|  | si $=<3,70>$ <br> $k=49$ |
| si.push $(k) ;$ |  |
|  |  |

## Example

| Code | State |
| :--- | :--- |
|  | si $=<3,70>$ <br> $k=49$ |
| si.push $(k) ;$ | si $=<49,3,70>$ <br> $k=49$ |
|  |  |

## Example

Note the alias created here, which you cannot see in the tracing table; you should be able to draw the appropriate diagram showing it.


## pop

T pop()

- Removes and returns the entry at the top (left end) of this.
- Updates: this
- Requires:
this /= < >
- Ensures:
\#this $=$ <pop> * this


## Example

| Code | State |
| :---: | :---: |
| $z=$ si.pop (); | si $=<49,3,70>$ <br> $z=-584$ |
| $z=$ |  |
|  |  |

## Example

| Code | State |
| :---: | :--- |
|  | si $=<49,3,70>$ <br> $z=-584$ |
| $z=$ si.pop(); | si $=<3,70>$ <br> $z=49$ |
|  |  |

## length

int length()

- Reports the length of this.
- Ensures:

$$
\text { length }=\mid \text { this } \mid
$$

## top

T top()

- Returns the entry at the the top (left end) of this.
- Aliases: reference returned by top
- Requires:
this /= < >
- Ensures:
<top> is prefix of this


## Example

| Code | State |
| :---: | :---: |
|  | si $=<49,3,70>$ <br> $k=-58$ |
| $k=$ si.top (); |  |
|  |  |

## Example

| Code | State |
| :---: | :--- |
|  | si $=<49,3,70>$ <br> $k=-58$ |
| $k=$ si.top (); | si $=<49,3,70>$ <br> $k=49$ |
|  |  |

## Example

Note the alias created here, which you cannot see in the tracing table; you should be able to draw the appropriate diagram showing it.

## State

$$
\begin{aligned}
& s i=<49,3,70> \\
& k=-58
\end{aligned}
$$

$$
s i=<49,3,70\rangle
$$

$$
k=49
$$

## replaceTop

T replaceTop (T x)

- Replaces the top of this with $x$, and returns the old top.
- Aliases: reference x
- Updates: this
- Requires:
this /= < >
- Ensures:

$$
\begin{aligned}
& \text { <replaceTop> is prefix of \#this and } \\
& \text { this }=\langle x\rangle * \text { \#this [1, |\#this|) }
\end{aligned}
$$

## Example

| Code | State |
| :---: | :--- |
|  | si $=<49,70>$ <br> $k=-58$ <br> $j=16$ |
| $k=$ si.replaceTop (j); |  |
|  |  |

## Example

| Code | State |
| :---: | :--- |
|  | si $=<49, ~ 70 \quad>$ <br> $k=-58$ <br> $j=16$ |
| $k=$ si.replaceTop (j); |  |
|  | si $=<16, ~ 70 \quad>$ <br> $k=49$ <br> $j=16$ |

## Example

Note the alias created here, which you cannot see in the tracing table; you should be able to

## State

 draw the appropriate diagram showing it.| N-s |  |
| :---: | :---: |
|  | $\begin{aligned} & s i=<16,70> \\ & k=49 \\ & j=16 \end{aligned}$ |

## Another Example

| Code | State |
| :---: | :---: |
|  | si $=<49,70>$ <br> $j=16$ |
| $j=$ si.replaceTop (j); |  |
|  |  |

## Another Example

| Code | State |
| :---: | :--- |
|  | si $=<49,70>$ <br> $j=16$ |
| $j=$ si.replaceTop(j); |  |
|  | si $=<16,70>$ <br> $j=49$ |

## Another Example

| This use of the method <br> avoids creating an alias: it <br> swaps $j$ with the entry <br> previously at the top. | State |
| :--- | :--- |
| $j=$ si.replaceTop (j); | si $=<49,70>$ <br> $j=16$ |
|  | si $=<16,70>$ <br> $j=49$ |

## flip

void flip()

- Reverses ("flips") this.
- Updates: this
- Ensures:
this = rev(\#this)


## Example

| Code | State |
| :---: | :---: |
|  | $s 1=<18,6,74>$ |
| sl.flip (); |  |
|  |  |

## Example

| Code | State |
| :---: | :---: |
|  | $s 1=<18,6,74>$ |
| sl.flip(); | $s 1=<74,6,18>$ |
|  |  |

## Resources

- OSU CSE Components API: Stack
- http://web.cse.ohio-state.edu/software/common/doc/

